

2/27/15 Ken Intriligator's Phys 4D Lecture outline

- A bit of history on the speed of light. Experiments: Galileo  $\sim 1618$  using eclipses of Jupiter's moon for the clock,  $c \approx \infty$ ; Cassini and Romer  $\sim 1676$ ,  $c \neq \infty!$ , takes light about 10 minutes to travel 1au; Huygens, light travels about 16.6 earth diameters per second; 1809 Delambre found it takes light about 8 minutes and 12 seconds to travel 1 au (actual value is about 8 minutes and 19 seconds, pretty close!); Fizeau, direct measurement on earth 1849, got actual answer to within 5%(!). Theory: Maxwell  $\sim 1862$   $c = 1/\sqrt{\mu_0\epsilon_0}$ .

- Recall Doppler effect for sound:  $\omega_{listener} = \omega_{source}(1 - (v_{source}/v_s))/(1 + (v_{listener}/v_s))$ . Not symmetric, since sound has a preferred frame: the rest frame of the air. Relativistic Doppler effect:  $\omega = \omega' \sqrt{(1 + \beta)/(1 - \beta)}$ . Let's see why.

- $x^\mu = (ct, x, y, z)$  is an example of a 4-vector, and every 4-vector transforms the same way between Lorentz frames:

$$\begin{pmatrix} a^0 \\ a^1 \\ a^2 \\ a^3 \end{pmatrix} = \begin{pmatrix} \gamma & \beta\gamma & 0 & 0 \\ \beta\gamma & \gamma & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} a^{0'} \\ a^{1'} \\ a^{2'} \\ a^{3'} \end{pmatrix}$$

Then  $a \cdot b \equiv a^0 b^0 - \vec{a} \cdot \vec{b}$  is the same in both frames, i.e. Lorentz (boost) invariant.

- $k^\mu \equiv (\omega/c, \vec{k})$  is an example of a 4-vector. Nice: therefore  $k \cdot x = \omega t - \vec{k} \cdot \vec{x} = \omega' t' - \vec{k}' \cdot \vec{x}'$ , and this is exactly the argument of a traveling wave  $\sim \cos(\vec{k} \cdot \vec{x} - \omega t)$ , so all observers properly agree upon the spacetime points where the wave has its highs and lows. Also  $k \cdot k = k' \cdot k'$ . For a light wave,  $\omega = ck$  means  $k \cdot k = 0$ , so all observers properly agree on that. Now use Lorentz transformation to get relation between  $\omega$  and  $\omega'$ .

- Fizeau was amazing! In 1851 he measured the speed of light through moving water!  $u_{expected} = (c/n) + v$ ,  $u_{observed} \approx (c/n) + v(1 - n^{-2})$  supported the "partial frame dragging" hypothesis. Derive from Lorentz transform:  $u_{actual} = ((c/n) + v)(1 + v/nc)^{-1} \approx u_{observed}$ .

- Next topic: energy-momentum 4-vector  $p^\mu = (E/c, \vec{p})$ .