

Homework 7, due Nov. 16, 2006

1. Suppose you flip 1000 unbiased coins.
  - (a) What is the probability of getting 500 heads and 500 tails? (Use Stirling's approximation.)
  - (b) What is the probability of getting 450 heads and 550 tails? (Use Stirling again.)
  - (c) Compute the above two probabilities using the Gaussian approximation. How do they compare?
  - (d) Compute  $\ln \Omega$  and  $\ln \omega_{max}$ . How do they compare?
  
2. Suppose that a system has allowed energy levels  $n\epsilon$ , with  $n = 0, 1, 2, 3, 4, \dots$ . There are three distinguishable particles, with total energy  $U = 4\epsilon$ .
  - (a) Tabulate all possible distributions of the three particles among the energy levels, satisfying  $U = 4\epsilon$ .
  - (b) Evaluate  $\omega_i$  for each of above distributions, and also  $\Omega = \sum_i \omega_i$ .
  - (c) Calculate the average occupation numbers  $\bar{N}_n = \sum_k N_{nk} \omega_k / \Omega$  for the three particles in the energy states. Here  $N_n$  is the average occupation number of the energy level with energy  $n\epsilon$ . You should find  $N_n$  for all  $n \leq 4$  (and find that  $N_{n>4} = 0$ ).
  
3. A drunk guy is walking along the  $x$  axis. He starts at  $x = 0$ , and his step size is  $L = 0.5$  meters. For each step, he has chance  $2/3$  of walking forwards (positive  $x$ ) and chance  $1/3$  of walking backwards (negative  $x$ ). What is his expected position,  $\bar{x}$ , after 50 steps? What is the expected RMS variation around  $\bar{x}$ ,  $\Delta x_{RMS} = \sqrt{\overline{(x - \bar{x})^2}}$  after 50 steps?